

# Micro fluidized beds: Wall effect and operability

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Received 16 November 2006; received in revised form 14 April 2007; accepted 24 April 2007

## Abstract

The minimum fluidization and minimum bubbling velocities of silica sand particles in air-blown micro beds of 120 mm high and with inner diameters of less than 32 mm were investigated to understand the wall effect in micro fluidized beds (MFBs) and the operability of the MFBs. Experimental results demonstrated that both the quoted velocities obviously increase with decreasing the inner diameter of the bed. A specific wall effect determined as the pressure drop per unit volume of particle bed in excess of the predicted pressure drop from the Ergun equation was proposed to quantitatively account for the influence of bed wall friction. By characterizing the fluidization qualities of differently sized particles in different MFBs, the article suggested further an optimal combination of bed diameter and particle size in the range of the static bed heights from 20 to 50 mm for the so-called micro fluidized bed (MFB) reactor devised to perform reaction(s) with minimal suffering from external gas mixing and gas diffusion.

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**Keywords:** Wall effect; Gas–solid flow; Micro fluidized bed; Minimum fluidization velocity; Minimum bubbling velocity

## 1. Introduction

With more fluidized bed reactors being introduced into laboratory fundamental studies, miniaturization of fluidized beds is receiving increasing interest because a small-size bed has good operability and availability for some particularly required characteristics. The concept of micro fluidized beds (MFBs) was first put forward by Potic et al. [1] to refer to the beds with inner diameters of a few millimeters. What promotes the present study is accurate measurement of reaction kinetics of solid reactants, which is difficult to be performed in Thermal Gravimetric Analyzer (TGA). In TGA, a solid reactant has to be loaded into a sample cell before the chamber encasing the cell is heated. Thus, any reaction or physical variation of the reactant has to occur during heating, making TGA unable to measure accurately the reaction rate of the solid reactant at arbitrary temperatures. On the other hand, the reaction itself in the sample cell of a TGA may suffer seriously from external gas diffusion. But, a fluidized bed (FB) reactor may be free of the above-mentioned problems,

which has thus been widely used to measure the rates of reactions such as pyrolysis, gasification, decomposition and so on. The FB reactor not only allows on-line feed of solid reactants at a preset temperature but diminishes also the gas-to-particle external diffusion with its flow turbulence, gas-particle shearing and particle-particle interaction. However, so far the employed FBs for studies of reaction kinetics generally have too large sizes, such as with an inner diameter above 50 mm and a bed height of a few hundreds of millimeters. This leads to serious gas mixing inside the reactor, causing the measured kinetic data based on changes of effluent gas composition to seriously deviate from real values. As a result, we are expecting to decrease this deviation to the utmost extent by replacing the fixed-bed reactor in TGA with a MFB reactor.

The fluidization characteristics (of a given kind of particles) in MFBs should be different from those in the ordinary-size fluidized beds due to much strong the wall effect in MFBs. From the viewpoint of operating and controlling a MFB kinetic analyzer, knowing the minimum fluidization and minimum bubbling velocities ( $U_{mf}$  and  $U_{mb}$ ) enables us to determine the suitable gas velocities for the analyzer so that the fluidization in the MFB reactor can be maintained in its desirable state. Therefore, the present article is devoted to investigating  $U_{mf}$  and  $U_{mb}$  of silica sand particles in MFBs with inner diameters less than 32 mm and a bed height of 120 mm to throw more light on the

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## Nomenclature

$A$	cross-sectional area of the bed ( $\text{m}^2$ )
$d_p$	particle diameter (m)
$D_t$	bed diameter (m)
$g$	gravitational acceleration ( $\text{m/s}^2$ )
$H_B$	bed height (m)
$H_s$	static bed height (m)
$m$	mass of the particles in the bed (kg)
$N$	the number of samples
$U_c$	critical gas velocity (m/s)
$U_g$	superficial gas velocity (m/s)
$U_{mb}$	minimum bubbling velocity (m/s)
$U_{mf}$	minimum fluidization velocity (m/s)
$V_B$	volume of particle bed ( $\text{m}^3$ )
$\Delta P_0$	pressure drop across the gas distributor (Pa)
$\Delta P_B$	pressure drop across the particle bed (Pa)
$\Delta P_{\text{Ergun}}$	pressure drop across the fixed bed (Pa)
$\Delta P_w$	extra pressure drop resulting from the wall (Pa)
$\Delta \bar{P}_B$	averaged pressure drop across the bed (Pa)
$\varepsilon$	bed voidage
$\rho_b$	bulk density of the particles ( $\text{kg/m}^3$ )
$\rho_g$	density of the gas ( $\text{kg/m}^3$ )
$\rho_s$	real density of the particles ( $\text{kg/m}^3$ )
$\phi_s$	shape factor of the particles
$\mu$	viscosity of the gas (Pa s)
$\sigma_P$	standard deviation of pressure fluctuation at fluidization (Pa)

wall effect prevailing in the MFBs. By comparing the propensities to form gas channeling and particle slugging/plugging of differently sized particles in different MFBs under the operating conditions in this study, the article will find out further a suitable bed-particle combination for the use in MFB kinetic analyzers.

## 2. Experimental

### 2.1. Experimental set-up and procedure

A schematic diagram of experimental set-up is shown in Fig. 1. All experiments were carried out in three cylindrical quartz glass MFBs with a height of 120 mm and inner diameters ( $D_t$ ) of 12, 20 and 32 mm, respectively. The top of every bed could be opened to accept particle load before experiment but was closed with a ground glass stopper in test. A sintered plate of 5 mm in thickness made from 150- $\mu\text{m}$  silica sand particles was used as the MFB's gas distributor. As the outlet of the bed, there was a side tube of 10 mm i.d. on the top of every MFB, wherein another sintered plate was fixed with stuffed silica wool to prevent entrainment of fine particles with released gas. Air was used as the fluidizing gas and its flow rate was controlled with a mass flowmeter (GR116-1-A-PO&3, 5 LPM, Fathom Technologies, USA). The pressure drop across the bed was monitored with a differential pressure transducer (CP101/102PO&500, 1000, 2000 Pa, KIMO Instruments, France). All data were recorded

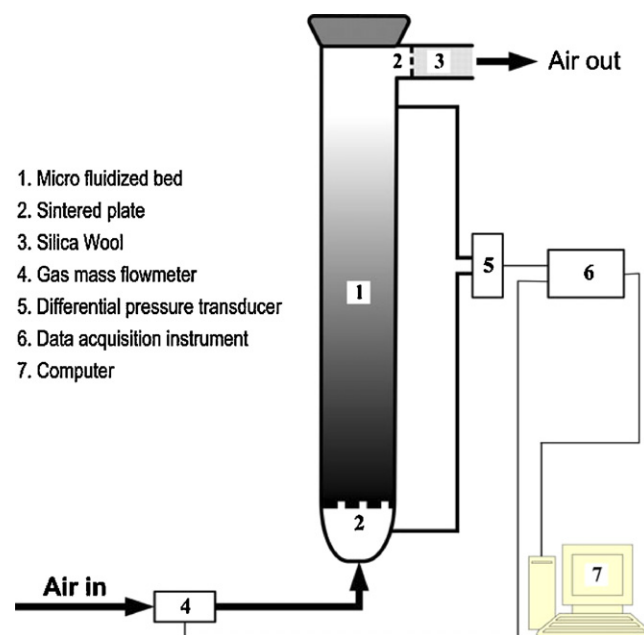


Fig. 1. Experimental set-up.

on a data acquisition instrument at a given sampling frequency and then transferred to a computer.

In order to examine the effect of particle sizes on fluidization behavior, three kinds of differently sized silica sand particles characterized in Fig. 2 were chosen as the fluidizing material. The pressure drops  $\Delta P_0$  across the distributor of each MFB at various superficial gas velocities measured in empty beds were shown in Fig. 3. By subtracting  $\Delta P_0$  from the total pressure drop across the fluidized bed, one can determine the pressure drop  $\Delta P_B$  across the particle bed. The sampling frequency was 100 Hz for all pressure signals and more than 10,000 points were taken in every measurement. In the course of all experiments, the superficial gas velocity  $U_g$  was first gradually increased at small intervals until the silica sand particles were fully fluidized. Then, the experiments continued by decreasing  $U_g$  back to zero. Three static bed heights,  $H_s = 20, 35$  and 50 mm, were investigated in three different MFBs, respectively. Both the total pressure drop and the bed height  $H_B$  were recorded as a function of  $U_g$  during all experiments.

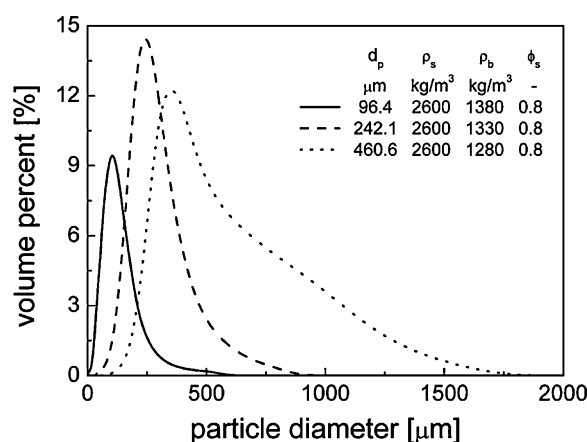


Fig. 2. Differential size distributions of three kinds of silica sand particles tested.

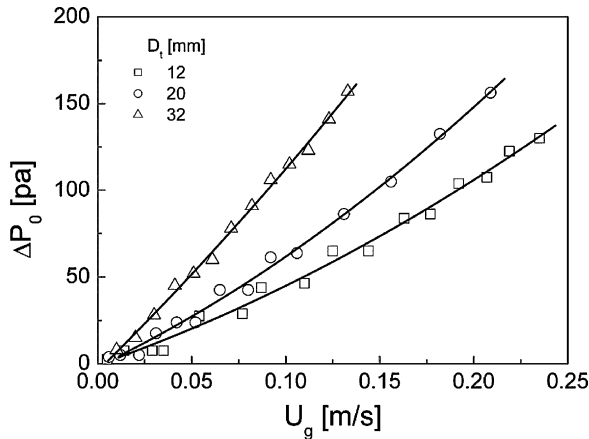


Fig. 3. Pressure drops across the distributor of each MFB at various superficial gas velocities.

## 2.2. Treatment of experimental data

The minimum fluidization velocity  $U_{mf}$  was generally defined as the gas velocity corresponding to the intersection of the pressure drop line for fixed bed with the horizontal line for fully fluidized bed. Loezos et al. [2] noted that some extra cohesive force between particles need to be overcome when increasing  $U_g$  to fluidize particles, which makes the measured  $U_{mf}$  much more unstable in  $U_g$ -ascending run than  $U_g$ -descending run [3]. Therefore, as exemplified by curve a in Fig. 4, we determined  $U_{mf}$  in  $U_g$ -descending run according to the Richardson's classic method [4].

The minimum bubbling velocity  $U_{mb}$  was determined generally by visually catching the first bubble appearing on the surface of the bed. However, the method is rather subjective, even infeasible in some cases. This is just the encounter of our tests. On the other hand, we found that the standard deviation  $\sigma_P$  of pressure fluctuation estimated from

$$\sigma_P = \left[ \frac{1}{n-1} \sum_{i=1}^n (\Delta P_{Bi} - \Delta \bar{P}_B)^2 \right]^{0.5} \quad (1)$$

evidently increases with the formation of obvious bubbles (see curve b in Fig. 4). Thus, in this study  $U_{mb}$  was defined from

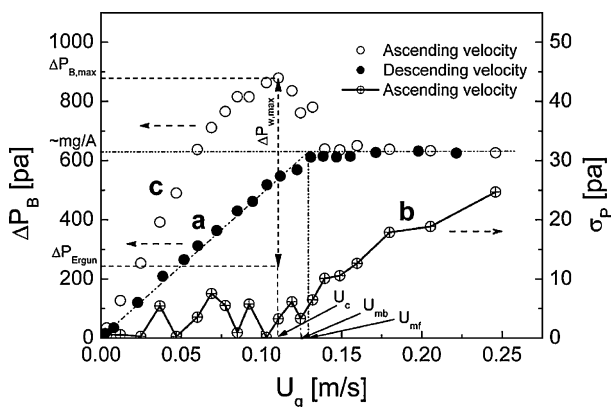


Fig. 4. Determination of  $U_{mf}$ ,  $U_{mb}$  and  $\Delta P_W$  in a typical operation ( $D_t = 12$  mm,  $d_p = 460.6$   $\mu\text{m}$  and  $H_s = 50$  mm).

the point whereat  $\sigma_P$  starts to increase continuously and quickly with increasing  $U_g$ . The definition implicates that stable bubbles smaller than the bed size would form continuously when  $U_g$  is beyond  $U_{mb}$ . From Fig. 4, it can be seen that the experimental  $U_{mb}$  is lower than the experimental  $U_{mf}$ . This may be explained by the fact that the sand particle of  $460.6$   $\mu\text{m}$  belonging to group B according to the Geldart classification was used as the fluidizing material in the experimental run, which led to the formation of the bubbles even before the minimum fluidization point since  $U_{mb}$  depends primarily on particle sizes but  $U_{mf}$  varies approximately with the square of particle sizes [5].

When  $U_g$  increases from zero to a critical value  $U_c$  (less than  $U_{mb}$ ), the pressure drop  $\Delta P_B$  across the particle bed may approach its maximum and becomes even greater than the weight of fluidized particles in the bed of unit cross-sectional area (see curve c in Fig. 4). Loezos et al. [2] found that this overpressure in gas–solid fluidization can be attributed primarily to the wall effect and the extent of overshoot pressure drop generally decreases with increasing bed sizes. Since the gas–solid system is still a fixed bed in the range of  $0 < U_g \leq U_c$ , its inherent pressure drop should be subject to the gas–particle friction calculated from the

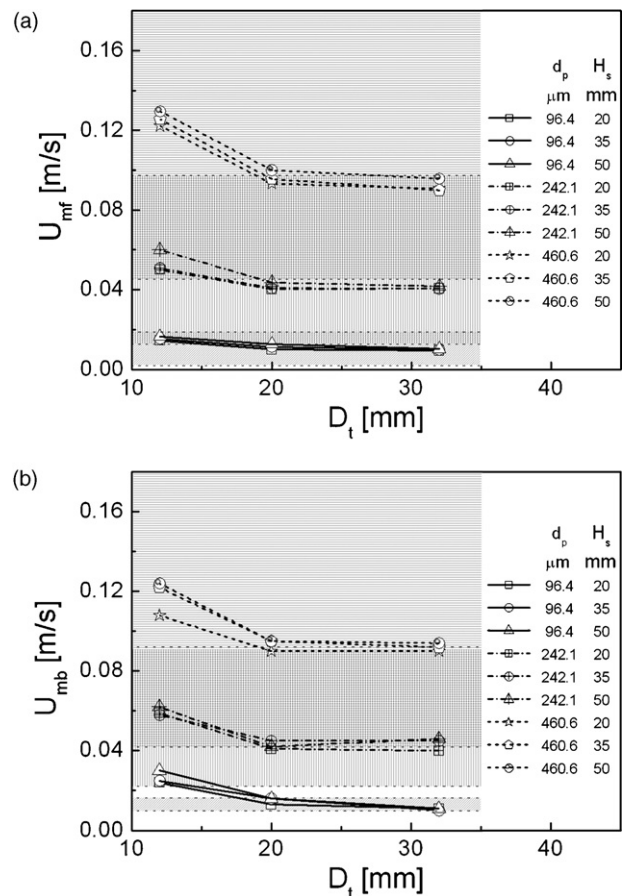


Fig. 5. Variations of (a)  $U_{mf}$  and (b)  $U_{mb}$  with  $D_t$  under different conditions (The shadow areas show the variation ranges of predicted  $U_{mf}$  and  $U_{mb}$  from literature correlations. The upper limits of the ranges for  $d_p = 460.6$   $\mu\text{m}$  are too large to show in the plot: ▨  $d_p = 96.4$   $\mu\text{m}$ ; ▩  $d_p = 242.1$   $\mu\text{m}$ ; ▤  $d_p = 460.6$   $\mu\text{m}$ ).

Ergun equation,

$$\frac{\Delta P_{\text{Ergun}}}{H_B} = 150 \frac{(1 - \varepsilon)^2}{\varepsilon^3} \frac{\mu U_g}{(\phi_s d_p)^2} + 1.75 \frac{1 - \varepsilon}{\varepsilon^3} \frac{\rho_g U_g^2}{\phi_s d_p} \quad (2)$$

The actually measured pressure drop  $\Delta P_B$  at a given  $U_g$ , on the other hand, is generally higher than  $\Delta P_{\text{Ergun}}$ . Hence, an extra pressure drop per unit volume of particle bed determined as

$$\frac{\Delta P_w}{V_B} = \frac{\Delta P_B - \Delta P_{\text{Ergun}}}{\pi D_t^2 H_B / 4} = \frac{\Delta P_B / H_B - \Delta P_{\text{Ergun}} / H_B}{\pi D_t^2 / 4} \quad (3)$$

can be used to quantify the specific strength of bed wall friction. In Eq. (2), the parameter  $\varepsilon$  refers to the average bed voidage calculated from

$$\varepsilon = 1 - \frac{H_s \rho_b}{H_B \rho_s} \quad (4)$$

### 3. Results and discussion

Fig. 5(a and b) shows the variations of  $U_{mf}$  and  $U_{mb}$  with  $D_t$  under all the tested conditions, respectively. Comparing these two figures demonstrates that for given  $D_t$  and  $H_s$  the experimental  $U_{mb}$  is generally greater than the experimental  $U_{mf}$  at  $d_p = 96.4 \mu\text{m}$  (Geldart A), but becomes very close to  $U_{mf}$  at  $d_p = 242.1 \mu\text{m}$  (Geldart B) and even less than  $U_{mf}$  at  $d_p = 460.6 \mu\text{m}$  (Geldart B). Many literature works have shown that  $U_{mb}$  is generally larger than  $U_{mf}$  for group A particles, but may be smaller than  $U_{mf}$  for group B particles [5,6]. The results

clarified in Fig. 5 comply with the literature observation, indicating in fact that the adopted definition of  $U_{mb}$  in this study is rational because the determination of  $U_{mf}$  involves rather a standard approach to make  $U_{mf}$  highly confident in all cases.

It can also be seen from Fig. 5 that static bed height  $H_s$ , as suggested by Broadhurst and Becker [7], has no observable effects on both  $U_{mf}$  and  $U_{mb}$  for all the tested  $d_p$  and MFBs. Both  $U_{mf}$  and  $U_{mb}$  decrease obviously with decreasing  $d_p$  and increasing  $D_t$ , but the decreasing degree of  $U_{mf}$  and  $U_{mb}$  with increasing  $D_t$  tends to decrease, even disappears when the bed diameter is large enough, for example, at  $D_t > 20 \text{ mm}$  for Fig. 5. A number of existing empirical correlations were selected to predict the  $U_{mf}$  [7–20] and  $U_{mb}$  [7,21–22] of the tested systems. The shadow areas in Fig. 5(a and b) show the variation ranges of the resulting  $U_{mf}$  and  $U_{mb}$ , respectively. Most of the experimental measurements fall in the ranges of the predicted values, but the experimental values from  $D_t = 12 \text{ mm}$  exceed the upper limit of the predictions. Hence, the existing literature correlations for  $U_{mf}$  and  $U_{mb}$  are probably applicable to the beds with inner diameters over 20 mm, but they evidently underestimate both the parameters in rather smaller beds. The implied essence is that the literature correlations, which were from larger beds, are unable to reproduce the wall effect prevailing in the beds with inner diameters below 20 mm.

Loezos et al. [2] suggested that the extent of pressure drop overshoot determined as  $(\Delta P_B A / mg - 1)$  quantitatively represents the strength of the wall effect. However, the physical meaning of  $(\Delta P_B A / mg - 1)$  is somewhat ambiguous because the

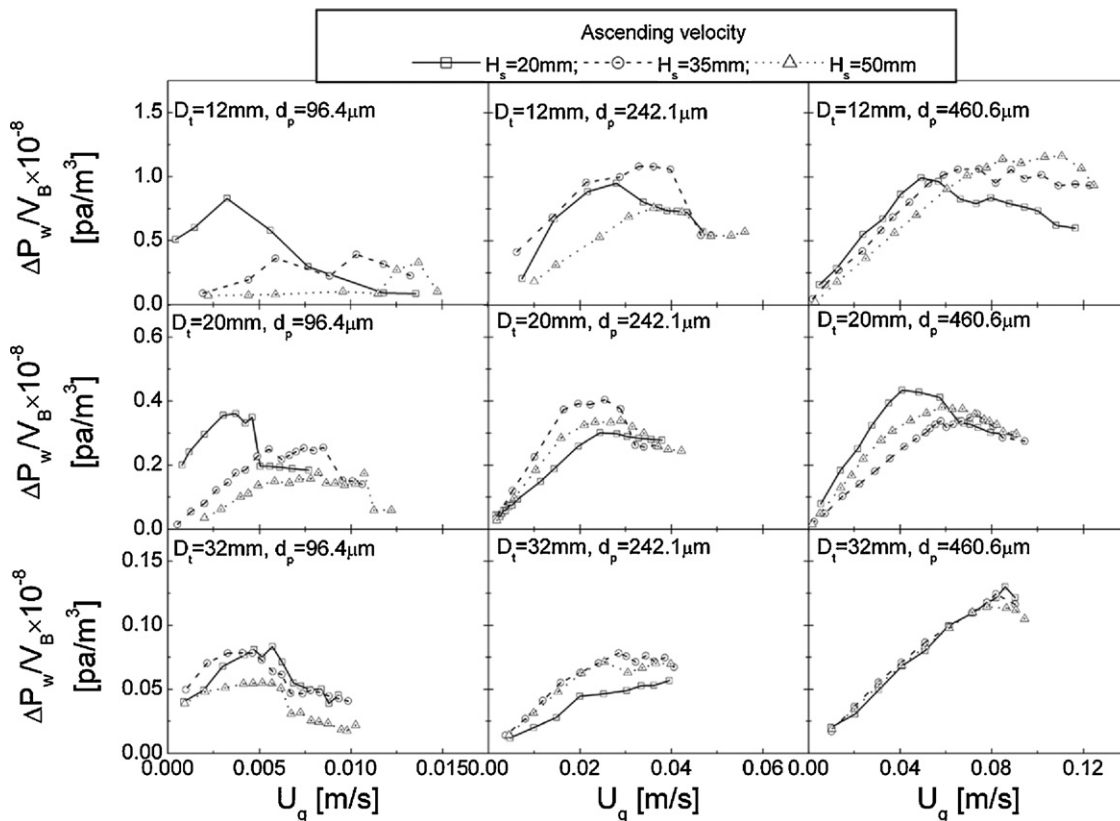


Fig. 6. Variations of  $\Delta P_w/V_B$  with  $U_g$  under different  $H_s$ ,  $D_t$  and  $d_p$ .



pressure drop overshoot occurs before the particles in the bed are completely fluidized, whereas the real pressure drop without wall effect is not  $mg/A$  but is subject to the friction estimated with, for example, the Ergun equation. Following this concern, we thus defined the parameter  $\Delta P_w/V_B$  shown in Eq. (3). As shown in Fig. 6, this parameter varies with  $U_g$  under the condition of  $U_g < U_{mf}$ , and at  $U_g = U_c$  it reaches a maximum estimated as

$$\frac{\Delta P_{w,max}}{V_B} = \frac{(\Delta P_B/H_B - \Delta P_{Ergun}/H_B)_{U_g=U_c}}{\pi D_t^2/4} \quad (5)$$

Noting that  $\Delta P_{w,max}/V_B$  represents the maximum extra pressure drop per unit volume of particle bed induced by the bed wall, we think that this newly defined parameter could provide an alternatively new measure to the wall-effect-induced extra barrier that should be overcome for the particles to be fully fluidized in a bed. Fig. 7 reveals that  $\Delta P_{w,max}/V_B$  decreases with increasing  $D_t$  under all tested operating conditions, but may be anticipated to vary little with  $d_p$  and  $H_s$  when the inner diameter of the MFB is greater than 20 mm. The result reasonably accounts for the decrease of  $U_{mf}$  with increasing  $D_t$  and the little effect of  $H_s$  on  $U_{mf}$  clarified in Fig. 5(a). But in the MFBs with inner diameters below 20 mm, the maximum extra pressure drop  $\Delta P_{w,max}$  may increase with increasing both  $d_p$  and  $H_s$  because large particles and great static bed heights lead to much serious slugging and more stronger particle-wall interaction. Therefore,

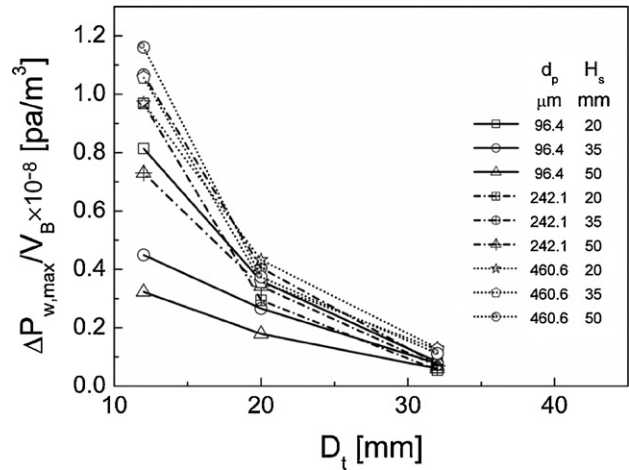


Fig. 7. Variations of  $\Delta P_{w,max}/V_B$  with  $D_t$  under different  $H_s$  and  $d_p$ .

as shown in Fig. 7, in the MFB of i.d. = 12 mm an increase of  $d_p$  generally results in increasing  $\Delta P_{w,max}/V_B$ , but the effect of  $H_s$  on  $\Delta P_{w,max}/V_B$  is not obvious due to the proportional variation of  $V_B$  with  $H_s$ .

Fig. 8 reproduces the standard deviation  $\sigma_P$  of pressure signals measured across all the tested MFBs. The deviation  $\sigma_P$  generally increases with increasing  $d_p$  and  $H_s$  and is lower for larger  $D_t$  under a given  $U_g$ . Meanwhile, the degree that  $\sigma_P$

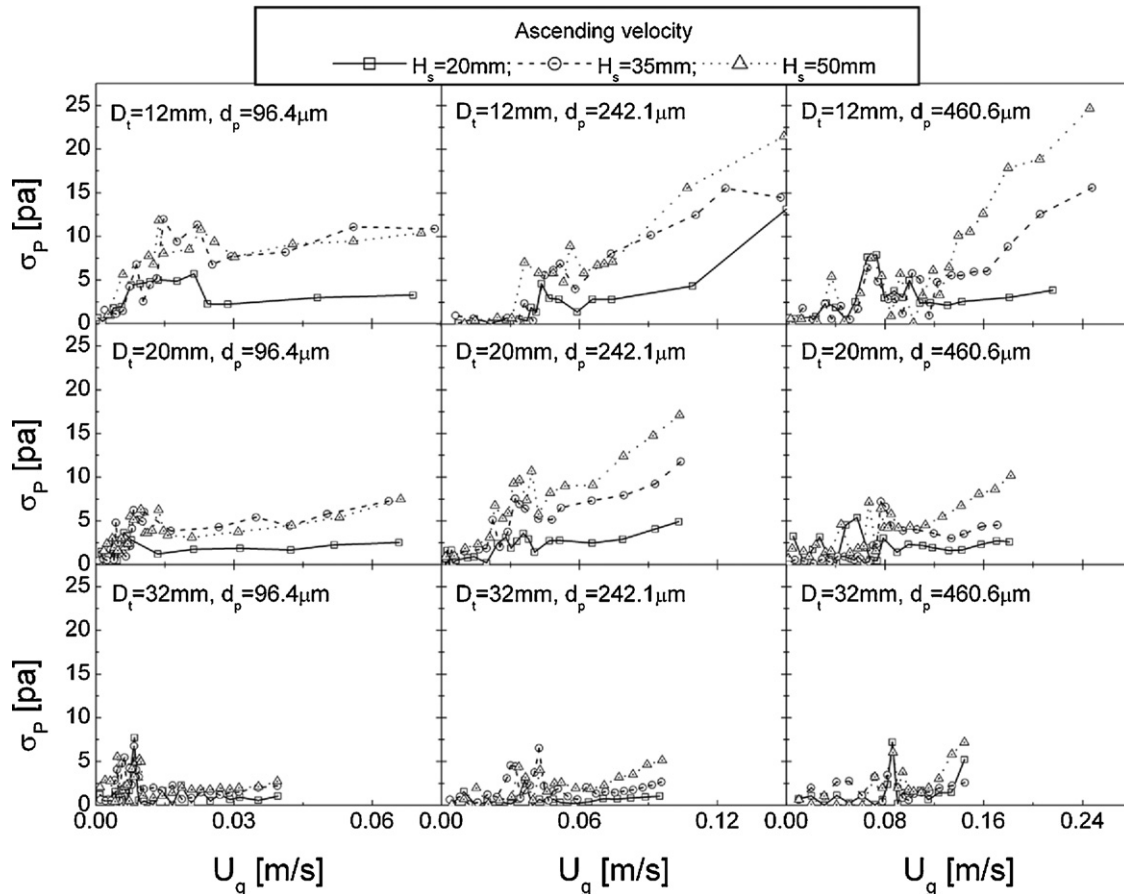


Fig. 8. Variations of  $\sigma_P$  with  $U_g$  at  $U_g$ -ascending tests under different conditions.

increases with increasing  $U_g$  is higher for smaller  $D_t$  and larger  $d_p$ . All of these features justify the variations of bubbling characteristics with bed diameters and particle sizes. That is, the larger particles likely lead to larger bubbles, while the bubbling flow in a smaller bed tends to present as the slugging/plugging type. Therefore, the minimum bubbling velocity  $U_{mb}$  tends to increase with increasing  $d_p$  and decreasing  $D_t$ , as shown in Fig. 5(b). In fact, the experiments also showed that slugging fluidization occurs obviously in the MFB of i.d. = 12 mm under the operating conditions, whereas gas channeling may happen in the bed of i.d. = 32 mm when  $U_g$  ranges from zero to about  $1.5U_{mf}$ . As shown in Fig. 3, the pressure drop  $\Delta P_0$  of the gas distributor in the MFB of i.d. = 32 mm is much greater than that in the other two smaller MFBs for the same  $U_g$ . That is, there should not exist nonuniform distribution of the gas flow in the MFB of i.d. = 32 mm since the same particles can be fluidized homogeneously and stably in the MFB of i.d. = 20 mm under the same operating conditions. So, the gas channeling occurring in the MFB of i.d. = 32 mm may be attributed to a relative low  $U_g$  in this study. Just because of this gas channeling, in Fig. 8  $\sigma_P$  is higher for fixed bed than for fluidized bed in the case of i.d. = 32 mm (third row). Certainly, neither slugging fluidization nor gas channeling is favorable to the bed intended to be employed as a fluidized bed reactor. In the view of selecting a suitable bed–particle combination for the use as a micro fluidized bed reactor, we hence suggest that the MFB of i.d. = 20 mm with silica sand particles of  $d_p = 242.1 \mu\text{m}$  in the range of the static bed heights from 20 to 50 mm should be the best choice due to stable and homogeneous fluidization for this system.

#### 4. Conclusions

- In micro fluidized beds (MFBs) with inner diameters of 10–32 mm the minimum fluidization velocity can be determined with the same method used ever for the other large-size beds, but the determination of the minimum bubbling velocity through the usually adopted visual observation of the appearance of the first gas bubble is rather difficult.
- The minimum fluidization and minimum bubbling velocities both exhibited an evident decrease when increasing the bed diameter from 12 to 20 mm. Above 20 mm the bed diameter only slightly affected such two velocities. Consequently, the article suggested that the bed wall effect may be extremely significant in the 12 mm bed.
- Through defining and calculating the extra pressure drop per unit bed volume in excess of that calculated from the Ergun equation, the bed wall effect in MFBs was found to decrease with increasing the bed diameter, but has little relation with both particle size and static bed height when the bed diameter is greater than 20 mm.
- A bed of an i.d. of about 20 mm was suggested to be suitable for the silica sand particles of  $242.1 \mu\text{m}$  in the range of the

static bed heights from 20 to 50 mm to make the bed relatively stably and homogeneously fluidized to be eligible for a MFB reactor. The MFB reactor is believed effective for suppressing external gas mixing and diffusion to make it suitable for reaction kinetics measurement.

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